# Chapter 31: Nuclear Applications

#### **Practice Problems**

#### page 642

- The carbon isotope, 12C, has a nuclear mass of 12.0000 u.
  - a. Calculate its mass defect.

6 protons = 
$$(6)(1.007825 \text{ u}) = 6.046950 \text{ u}$$
  
6 neutrons =  $(6)(1.008665 \text{ u}) = 6.051990 \text{ u}$   
total 12.098940 u  
mass of carbon nucleus  $-12.000000 \text{ u}$   
mass defect 0.098940 u

b. Calculate its binding energy in MeV.

(0.098940 u)(931.49 MeV/u) = 92.162 MeV

- 2. The isotope of hydrogen that contains 1 proton and 1 neutron is called deuterium. The mass of its nucleus is 2.0140 u.
  - a. What is its mass defect?

$$\begin{array}{rcl} 1 \; \text{proton} = & 1.007825 \; \text{u} \\ 1 \; \text{neutron} = & & \frac{1.008665}{2.016490} \; \text{u} \\ \text{mass of deuterium nucleus} = & -\frac{2.0140}{0.0025} \; \text{u} \\ \end{array}$$

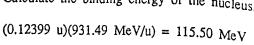
b. What is the binding energy of deuterium in MeV?

(0.0025 u)(931.49 MeV/u) = 2.3 MeV

- A nitrogen isotope, 15N, has 7 protons and 8 neutrons. Its nucleus has a mass of 15.00011 u.
  - a. Calculate the mass defect of this nucleus.

#### Practice Problems

b. Calculate the binding energy of the nucleus.



- An oxygen isotope, 16O, has a nuclear mass of 15.99491 u.
  - a. What is the mass defect of this isotope?

8 protons = 
$$(8)(1.007825 \text{ u})$$
 =  $8.062600 \text{ u}$   
8 neutrons =  $(8)(1.008665 \text{ u})$  =  $8.069320 \text{ u}$   
total  $16.131920 \text{ u}$   
mass of oxygen nucleus  $-15.99491 \text{ u}$   
mass defect  $0.13701 \text{ u}$ 

b. What is the binding energy of its nucleus?

$$(0.13701 \text{ u})(931.49 \text{ MeV/u}) = 127.62 \text{ MeV}$$

#### page 645

Use Table C-5 of the Appendix to complete the following nuclear equations.

a. 
$${}^{14}_{6}C \rightarrow ? + {}^{0}_{-1}e$$

$${}^{14}_{6}C \rightarrow {}^{14}_{7}N + {}^{0}_{-1}e$$

b. 
$${}^{55}_{24}\text{Cr} \rightarrow ? + {}^{0}_{-1}e$$

$$^{55}_{24}{\rm Cr} \, \rightarrow \, ^{55}_{25}{\rm Mn} \, + \, ^{0}_{-1}e$$

6. Write the nuclear equation for the transmutation of a uranium isotope, 238U, into a thorium isotope, <sup>234</sup>Th, by emission of an alpha particle.

A radioactive polonium isotope, <sup>214</sup>Po, undergoes Write the alpha decay and becomes lead. nuclear equation.

$$^{214}_{84}Po \rightarrow ^{210}_{82}Pb + ^{4}_{2}He$$



SEE SEE V

#### Practice Problems

- Write the nuclear equations for the beta decay of these isotopes.
  - a. 210Pb

$$^{210}_{82}Pb \rightarrow ^{210}_{83}Bi + ^{0}_{12}e$$

b. 210Bi

$$^{210}\text{Bi} \rightarrow ^{210}\text{Po} + ^{0}\text{e}$$

c. 234Th

$$^{234}_{90}$$
Th  $\rightarrow ^{234}_{91}$ Pa +  $^{0}_{1}e$ 

d. 239Np

$$^{239}_{93}Np \rightarrow ^{239}_{94}Pu + ^{9}_{9}e$$

#### page 652

a. Calculate the mass defect for the deuteriumtritium fusion reaction used in the Tokamak,  $^{2}H + ^{3}H \rightarrow ^{4}He + ^{1}n.$ 

> Input masses 2.014102 u + 3.016049 u = 5.030151 u.Output masses 4.002603 u + 1.008665 u

> = 5.011268 u.

Difference is 0.018883 u

b. Find the energy equivalent of the mass defect.

(0.018883 u)(931.49 MeV/u) = 17.589 MeV

Calculate the energy released for the overall reaction in the sun where four protons produce one 4He, two positrons, and two neutrinos.

### Practice Problems

Positron mass =  $(9.109 \times 10^{-31} \text{ kg}) \left[ \frac{1 \text{u}}{1.661 \times 10^{-27} \text{ kg}} \right]$ = 0.000548 uInput mass: 4 protons = 4(1.007825 u)= 4.031300 uOutput mass:  ${}_{2}^{4}$ He + 2 positrons = 4.002603 u + 2(0.000548 u)= 4.003699 Mass difference = 0.027601 uEnergy released = (0.027601 u)(931.49 MeV/u)= 25.710 MeV

## Chapter Review Problems

pages 654-655

- 1. A carbon isotope, 13C, has a nuclear mass of 13.00335 u.
  - a. What is the mass defect of this isotope?

6 protons = 
$$(6)(1.007825 \text{ u}) = 6.046950 \text{ u}$$
  
7 neutrons =  $(7)(1.008665 \text{ u}) = \frac{7.060655 \text{ u}}{13.107605 \text{ u}}$   
mass of carbon nucleus  $\frac{13.107605 \text{ u}}{13.00335 \text{ u}}$   
mass defect  $\frac{13.00335 \text{ u}}{10.10426 \text{ u}}$ 

- b. What is the binding energy of its nucleus? (0.10426 u)(931 MeV/u) = 97.1 MeV
- A nitrogen isotope, 14N, has a nuclear mass of approximately 14.00307 u.
  - a. What is the mass defect of the nucleus?

- b. What is the binding energy of this nucleus? (0.11236 u)(931 MeV/u) = 105 MeV
- c. What is the binding energy per nucleon?

$$Energy = \frac{105 \text{ MeV}}{14 \text{ nucleons}} = 7.5 \text{ MeV/nucleon}$$

- A nitrogen isotope, <sup>12</sup><sub>7</sub>N, has a nuclear mass of 12.0188 u.
  - a. What is the binding energy per nucleon?

7 protons = 
$$(7)(1.007825 \text{ u}) = 7.054775 \text{ u}$$
  
5 neutrons =  $(5)(1.008665 \text{ u}) = 5.043325 \text{ u}$   
total 12.098100 u  
mass of nitrogen-12 nucleus - 12.0188 u  
mass defect 0.0793 u

binding energy (0.0793 u)(931 MeV/u) = 73.8 MeVbinding energy per nucleon  $= \frac{73.8 \text{ MeV}}{12 \text{ nucleons}}$ 

= 6.15 MeV

b. Does it require more energy to separate a nucleon from a <sup>14</sup>/<sub>7</sub>N nucleus or from a <sup>12</sup>/<sub>7</sub>N nucleus? Refer to the previous problem.

It requires more energy to remove a nucleon from nitrogen - 14, 7.5 MeV.

4. The two positively-charged protons in a helium nucleus are separated by about 2.0 × 10<sup>-15</sup> m. Use Coulomb's law to find the electric force of repulsion between the two protons. The result will give you an indication of the strength of the strong nuclear force.

$$F = K \frac{qq'}{d^2}$$

$$= \frac{K(1.6 \times 10^{-19} \text{ C})(1.6 \times 10^{-19} \text{ C})}{(2.0 \times 10^{-15} \text{ m})^2}$$
= 58 N

### Chapter Review Problems

5. A  $^{232}_{92}$ U nucleus, mass = 232.0372 u, decays to  $^{228}$ Th, mass = 228.0287 u, by emitting an  $\alpha$  particle, mass = 4.0026 u, with a kinetic energy of 5.3 MeV. What must be the kinetic energy of the recoiling thorium nucleus?



mass defect = (232.0372 u) - (228.0287 u + 4.0026 u)= 0.0059 utotal KE = (0.0059 u)(931 MeV/u)

= 5.5 MeV

KE for thorium nucleus
= (5.5 MeV) - (5.3 MeV)

= 0.2 MeV

The binding energy for <sup>4</sup><sub>2</sub>He is 28.3 MeV.
 Calculate the mass of a helium nucleus in atomic mass units.

Mass defect 
$$\frac{28.3 \text{ MeV}}{931 \text{ MeV/u}} = 0.0304 \text{ u}$$

2 protons = 
$$(2)(1.007825 \text{ u}) = 2.015650 \text{ u}$$
  
2 neutrons =  $(2)(1.008665 \text{ u}) = 2.017330 \text{ u}$   
mass  $4.032980 \text{ u}$   
minus mass defect  $-0.0304 \text{ u}$   
 $4.0026 \text{ u}$ 

7. The radioactive nucleus indicated in each equation disintegrates by emitting a positron. Complete each nuclear equation.

a. 
$$^{21}_{11}$$
Na  $\rightarrow$  ? +  $^{0}_{+1}e$  + ?

$$^{21}_{11}Na \rightarrow ^{21}_{10}Ne + ^{0}_{+1}e + ^{0}_{0}v$$

b. 
$${}^{49}_{24}\text{Cr} \rightarrow ? + {}^{0}_{+1}e + ?$$

$$^{49}_{24}\text{Cr} \rightarrow ^{49}_{23}\text{V} + ^{0}_{+1}e + ^{0}_{0}v$$

8. Complete the nuclear equations for these transmutations.

a. 
$${}_{15}^{30}P \rightarrow ? + {}_{1}^{0}e + ?$$

$$^{30}P \rightarrow ^{30}Si + ^{0}e + ^{0}v$$

b. 
$${}^{205}_{82}Pb \rightarrow ? + {}^{0}_{*1}e + ?$$
  
 ${}^{205}_{82}Pb \rightarrow {}^{205}_{81}Tl + {}^{0}_{*1}e + {}^{0}_{0}v$ 

- 9. A mercury isotope, <sup>200</sup>Hg, is bombarded the deuterons, <sup>2</sup>H. The mercury nucleus absorbs the dueteron and then emits an alpha particle.
  - a. What element is formed by this reaction?

    Gold.
  - b. Write the nuclear equation for the reaction.

$$^{200}_{80}$$
Hg +  $^{2}_{1}$ H  $\rightarrow ^{198}_{79}$ Au +  $^{4}_{2}$ He

10. When bombarded by protons, a lithium isotope, <sup>7</sup><sub>3</sub>Li, absorbs a proton and then ejects two alpha particles. Write the nuclear equation for this reaction.

$${}_{3}^{7}\text{Li} + {}_{1}^{1}\text{H} \rightarrow 2{}_{2}^{4}\text{He}$$

11. Each of the nuclei given below can abosorb an alpha particle. Assume that no secondary particles are emitted by the nucleus. Complete each equation.

**a.** 
$${}^{14}_{7}N + {}^{4}_{2}He \rightarrow ?$$

$$^{14}N + _{2}^{4}He \rightarrow _{9}^{18}F$$

**b.** 
$$^{27}_{13}Al + ^{4}_{2}He \rightarrow ?$$

$$^{27}_{13}A1 + ^{4}_{2}He \rightarrow ^{31}_{15}P$$

12. In each of these reactions, a neutron is absorbed by a nucleus. The nucleus then emits a proton. Complete the equations.

**a.** 
$$^{65}_{29}$$
Cu +  $^{1}_{0}n \rightarrow ? + ^{1}_{1}H$ 

$$^{65}_{29}$$
Cu +  $^{1}_{0}n \rightarrow ^{65}_{28}$ Ni +  $^{1}_{1}$ H

**b.** 
$${}^{14}_{7}N + {}^{1}_{0}n \rightarrow ? + {}^{1}_{1}H$$

$${}^{14}_{7}N + {}^{1}_{0}n \rightarrow {}^{14}_{6}C + {}^{1}_{1}H$$

## Chapter Review Problems

- 13. When a boron isotope, <sup>10</sup><sub>5</sub>B, is bombarded with neutrons, it absorbs a neutron and then emits an alpha particle.
  - a. What element is also formed?
    Lithium.
  - b. Write the nuclear equation for this reaction.

$$^{10}_{5}B + ^{1}_{0}n \rightarrow ^{7}_{3}Li + ^{4}_{2}He$$

- 14. When a boron isotope, <sup>11</sup><sub>5</sub>B, is bombarded with protons, it absorbs a proton and emits a neutron.
  - a. What element is formed?

Carbon.

b. Write the nuclear equation for this reaction.

$${}^{11}_{5}B + {}^{1}_{1}p \rightarrow {}^{11}_{6}C + {}^{1}_{0}n$$

c. The isotope formed is radioactive, decaying by emitting a positron. Write the complete nuclear equation for this reaction.

$${}^{11}_{6}C \rightarrow {}^{11}_{5}B + {}^{0}_{1}e + {}^{0}_{0}v$$

- 15. The isotope most commonly used in PET scanners is  $^{18}_{9}F$ .
  - a. What element is formed by the positron emission of this element?

Oxygen.

b. Write the equation for this reaction.

$${}^{18}\text{F} \rightarrow {}^{18}\text{O} + {}^{0}\text{e} + {}^{0}\text{v}$$

c. The half-life of <sup>18</sup>/<sub>9</sub>F is 110 min. A solution containing 10.0 mg of this isotope is injected into a patient at 8:00 a.m. How much remains at 3:30 p.m.?

The time is about 4 half-lives, so

 $\frac{1}{16}$ (10.0 mg) or 0.63 mg remains.

16. The basements of many homes contain the rock granite or are built over granite. Granite contains small amounts of radioactive uranium and thorium. Uranium-238 goes through a series of decays before reaching a stable lead isotope.  $^{238}_{92}$ U emits an alpha, leaving an isotope that decays by emitting a beta. The next decay is again a  $\beta$ , follow by three  $\alpha$  decays. The result is the gas radon that can seep into the basement. Write the equations for these decays.

$$^{234}_{92}U \rightarrow ^{234}_{90}Th + ^{4}_{2}He$$

$$^{234}_{90}Th \rightarrow ^{234}_{91}Pa + ^{0}_{-1}e + ^{0}_{0}\overline{v}$$

$$^{234}_{91}Pa \rightarrow ^{234}_{92}U + ^{0}_{-1}e + ^{0}_{0}\overline{v}$$

$$^{234}_{92}U \rightarrow ^{230}_{90}Th + ^{4}_{2}He$$

$$^{230}_{90}Th \rightarrow ^{226}_{88}Ra + ^{4}_{2}He$$

<sup>226</sup>Ra → <sup>222</sup>Rn + <sup>4</sup>He

17. The first atomic bomb released an energy equivalent of 20 kilotons of TNT. One kiloton of TNT is the equivalent of  $5.0 \times 10^{12}$  J. What was the mass of the uranium-235 that was fissioned to produce this energy?

Energy = 
$$(20 \text{ kilotons})(5.0 \times 10^{12} \text{ J/kiloton})$$
  
=  $1.0 \times 10^{14} \text{ J}$ 

$$\frac{1.0 \times 10^{14} \text{ J}}{1.6 \times 10^{-19} \text{ J/eV}} = 6.3 \times 10^{32} \text{ eV}$$

$$\frac{(6.3 \times 10^{32} \text{ eV})}{(2.0 \times 10^{2} \text{ MeV/atom})(10^{6} \text{ eV/MeV})}$$

 $= 3.1 \times 10^{24} \text{ atoms}$ 

$$\frac{3.1 \times 10^{24} \text{ a t om s}}{6.02 \times 10^{23} \text{ atoms / mole}} = 5.2 \text{ moles}$$

(5.2 moles)(0.235 kg/mole) = 1.2 kg

18. Complete the following fission reaction.  $^{239}_{34}$ Pu +  $^{1}_{0}n \rightarrow ^{137}_{52}$ Te + ? +  $3^{1}_{0}n$ 

$$^{239}_{94}$$
Pu +  $^{1}_{0}$ n  $\rightarrow ^{137}_{52}$ Te +  $^{100}_{42}$ Mo +  $^{11}_{0}$ n

## Chapter Review Problems

19. Complete the following fission reaction 
$$^{235}_{92}U + ^{1}_{0}n \rightarrow ^{92}_{36}Kr + ? + 3^{1}_{0}n$$

$$^{235}_{92}U + ^{1}_{0}n \rightarrow ^{92}_{36}Kr + ^{141}_{56}Ba + 3^{1}_{0}n$$

20. Plutonium is formed in two steps. First U-238 absorbs a neutron which then becomes unstable U-239. The U-239 emits a beta particle forming a new element and this new element emits a second beta particle forming plutonium. Complete the following reaction

21. Complete each of the following fusion reactions.  ${}_{1}^{2}H + {}_{1}^{2}H \rightarrow ? + {}_{0}^{1}n$ 

$${}_{1}^{2}H + {}_{1}^{2}H \longrightarrow {}_{1}^{2} + {}_{1}^{1}H$$
 ${}_{1}^{2}H + {}_{1}^{3}H \longrightarrow {}_{2}^{2} + {}_{0}^{1}n$ 
 ${}_{1}^{2}H + {}_{1}^{2}H \longrightarrow {}_{2}^{3}He + {}_{0}^{1}n$ 
 ${}_{1}^{2}H + {}_{1}^{2}H \longrightarrow {}_{3}^{3}H + {}_{1}^{1}H$ 

 $^{239}_{93}Np \rightarrow ^{239}_{94}Pu + _{1}^{0}e + _{0}^{0}\bar{v}$ 

$$_{1}^{2}H + _{1}^{3}H \longrightarrow _{2}^{4}He + _{0}^{1}n$$

- 22. One fusion reaction is  $_{1}^{2}H + _{1}^{2}H \rightarrow _{2}^{4}He$ .
  - a. What energy is released during this reaction?

$$(2)(2.01410 \text{ u}) - (4.00263 \text{ u}) = 0.02557 \text{ u}$$
  
 $(0.02557 \text{ u})(931 \text{ MeV/u}) = 23.8 \text{ MeV}$ 

b. Deuterium exists as a diatomic, two atom, molecule. One mole of deuterium contains 6.02 × 10<sup>23</sup> molecules. Find the amount of energy released, in joules, in the fusion of one mole of deuterium molecules.

(23.8 MeV/molecule)  

$$\times$$
 (6.02  $\times$  10<sup>23</sup> molecules/mole)  
 $\times$  (1.6  $\times$  10<sup>-19</sup> J/eV)(10<sup>6</sup> eV/MeV)  
= 2.29  $\times$  10<sup>12</sup> J/mole

c. When one mole of deuterium burns, combined with oxygen chemically, it releases 2.9 × 10<sup>6</sup> J. How many moles of dueterium molecules would have to burn to release just the energy released by the fusion of one mole of deuterium molecules?

$$\frac{2.29 \times 10^{12} \text{ J}}{2.9 \times 10^{6} \text{ J/mole}} = 7.9 \times 10^{5} \text{ moles}$$

- 23. The energy released in the fission of one atom of  $^{235}_{92}$ U is  $2.00 \times 10^2$  MeV. One mole of uranium atoms,  $6.02 \times 10^{23}$  atoms, has a mass of 0.235 kg.
  - a. How many atoms are in 1.00 kg  $^{235}_{92}$ U?

$$\frac{(6.02 \times 10^{23} \text{ atoms/mole})(1.00 \text{ kg})}{(0.235 \text{ kg/mole})} = 2.56 \times 10^{24} \text{ atoms.}$$

**b.** How much energy would be released if all the atoms in 1.00 kg of  $^{235}_{92}$ U underwent fission?

$$(2.56 \times 10^{24} \text{ atoms/kg})(2.0 \times 10^{2} \text{ MeV/atom})(1.6 \times 10^{-19} \text{ J/ev})(10^{6} \text{ eV/MeV}) = 8.2 \times 10^{13} \text{ J}$$

c. A typical large nuclear reactor produces fission energy at a rate of 3600 MW. How many kilograms of <sup>235</sup>U are used each second?

$$\frac{3.0 \times 10^{9} \text{ J/s}}{8.2 \times 10^{13} \text{ J/kg}} = 3.7 \times 10^{-5} \text{ kg/s}$$

d. How much 235U would be used in one year?

$$(3.7 \times 10^{-5} \text{ kg/s})(3.15 \times 10^{7} \text{ s/y}) = 1.2 \times 10^{3} \text{ kg/y}$$

## Supplemental Problems (Appendix B)

- 1. The carbon isotope, <sup>12</sup>C, has a nuclear mass of 12.000 000 u.
  - a. What is the mass defect of this isotope?

$$^{12}\text{CC}$$
  $6(^{1}\text{P}) = 6(1.007 \ 825 \ \text{u}) = 6.046 \ 950 \ \text{u}$ 
 $6(^{1}\text{o}n) = 6(1.008 \ 665 \ \text{u}) = 6.051 \ 990 \ \text{u}$ 
total mass of nucleus 12.098 940 u

 $^{12}\text{CC} - 12.000 \ 000 \ \text{u}$ 
mass defect  $-0.098 \ 940 \ \text{u}$ 

b. What is the binding energy of its nucleus?

$$E = (931.5 \text{ MeV/u})(0.098 940 \text{ u})$$
  
= 92.16 MeV

## Supplemental Problems

- 2. The sulfur isotope,  $^{32}_{16}$ S, has a nuclear mass of 31.972 07 u.
  - a. What is the mass defect of this isotope?

$$16(_{1}^{1}P) = 16(1.007 825 u) = 16.125 20 u$$

$$16(_{0}^{1}n) = 16(1.008 665 u) = \underline{16.138 64} u$$

$$32.263 84 u$$

$$_{16}^{32}S = 31.972 07 u$$

$$\underline{32.263 84}$$

$$\underline{32.263 84}$$

$$\underline{32.263 84}$$

$$\underline{32.263 84}$$

$$\underline{32.263 84}$$

b. What is the binding energy of its nucleus?

$$E = (931.5 \text{ MeV/u})(0.291 77 \text{ u})$$
  
= 271.8 MeV

- The sodium isotope, <sup>22</sup><sub>11</sub>Na, has a nuclear mass of 21.994 44 u.
  - a. What is the mass defect of this isotope?

$$11(^{1}_{1}P) = 11(1.007 \ 825 \ u) = 11.086 \ 08 \ u$$

$$11(^{1}_{0}n) = 11(1.008 \ 665 \ u) = \underline{11.095 \ 32} \ u$$

$$22.181 \ 40 \ u$$

$$- \frac{22}{11}Na = 21.994 \ 44 \ u$$

$$\underline{22.181 \ 40}$$

$$mass \ defect - 0.186 \ 96 \ u$$

b. What is the binding energy of its nucleus?

$$E = (931.5 \text{ MeV/u})(0.18696 \text{ u})$$
  
= 174.2 MeV

c. What is the binding energy per nucleon?

$$\frac{174.2 \text{ MeV}}{22 \text{ nucleons}} = 7.916 \text{ MeV/nucleon}$$

### Supplemental Problems

The binding energy for Li is 39.25 MeV.
 Calculate the mass of the lithium-7 nucleus in atomic mass units.

$$3(_{1}^{1}P) = 3(1.007 \ 825 \ u) = 3.023 \ 475$$
  
 $3(_{0}^{1}n) = 4(1.008 \ 665 \ u) = 4.034 \ 660$   
mass defect =  $\frac{39.25 \ \text{MeV}}{931.5 \ \text{MeV/u}} = -0.042 \ 14$   
 $7.016 \ 00$ 

5. Write the complete nuclear equation for the positron decay of <sup>132</sup>Cs.

$$^{132}Cs \rightarrow _{+1}^{0}e + ^{132}Xe + ^{0}v$$

6. Complete the nuclear reaction:  ${}^{14}N + {}^{1}n \rightarrow ? {}^{1}p + ?$ 

$$^{14}N + ^{1}n \rightarrow ^{15}N \rightarrow ^{1}p + ^{14}C$$

7. Complete the nuclear reaction:  ${}^{65}_{00}$ Cu +  ${}^{1}_{0}$ n  $\rightarrow$  ?  $\rightarrow$   ${}^{1}_{1}$ p + ?

$$^{65}_{29}$$
Cu +  $^{1}_{0}n \rightarrow ^{66}_{29}$ Cu  $\rightarrow ^{1}_{1}p$  +  $^{65}_{29}$ Ni

8. When a magnesium isotope, <sup>24</sup><sub>12</sub>Mg, is bombarded with neutrons, it absorbs a neutron and then emits a proton. Write the complete nuclear equation for this reaction.

$$^{24}_{12}$$
Mg +  $^{1}_{0}$ n  $\rightarrow ^{25}_{12}$ Mg  $\rightarrow ^{1}_{1}$ p +  $^{24}_{12}$ Na

9. When oxygen-17 is bombarded by neutrons, it absorbs a neutron and then emits an alpha particle. The resulting nucleus is unstable and it will emit a beta particle. Write the complete nuclear equation for this reaction.

$$^{17}_{8}\mathrm{O} \, + \, ^{1}_{0}n \, \rightarrow \, ^{18}_{8}\mathrm{O} \, \rightarrow \, ^{4}_{2}\mathrm{He} \, + \, ^{14}_{6}\mathrm{C} \, \rightarrow \, ^{0}_{-1}e \, + \, ^{14}_{7}\mathrm{N} \, + \, ^{6}_{0}\bar{\upsilon}$$

10. Complete the following fission reaction:  $^{239}_{44}$ Pu +  $^{1}_{0}n \rightarrow ^{137}_{52}$ Te +  $3(^{1}_{0}n)$  + ?

$$^{239}_{94}$$
Pu +  $^{1}_{0}n \rightarrow ^{137}_{52}$ Te +  $3(^{1}_{0}n)$  +  $^{100}_{42}$ Mo



### Supplemental Problems

11. Complete the following fission reaction:  ${}^{233}U + {}^{1}n \rightarrow {}^{134}CS + 2({}^{1}n) + ?$ 

$$^{233}_{92}U + ^{1}_{0}n \rightarrow ^{134}_{55}Cs + 2(^{1}_{0}n) + ^{98}_{37}Rb$$

12. complete the following fission reaction:  ${}^{235}_{22}U + {}^{1}_{0}n \rightarrow {}^{90}_{38}Sr + 10({}^{1}_{0}n) + ?$ 

$$^{235}\text{U} + ^{1}\text{n} \rightarrow ^{90}\text{Sr} + 10(^{1}\text{n}) + ^{136}\text{Xe}$$

- 13. Strontium-90 has a mass of 89.907 747 u, xenon-136 has a mass of 135.907 221 u and uranium-235 has a mass of 235.043 915 u.
  - a. Compute the mass defect in the previous problem.

$$Sr-90 = 89.907 747 u$$

$$Xe-136 = 135.907 221 u$$

$$10(\ln n) = 10(1.008 665 u) = 10.086 65 u$$

$$= 235.901 62 u$$

$$\ln n = 1.008 665 u$$

$$U-235 = 235.043 915 u$$

$$= 236.052 580 u$$
mass defect = 235.90162 u - 236.05258 u
$$= -0.150 96 u$$

b. Compute the amount of energy released.

$$E = (931.5 \text{ MeV/u})(0.15096 \text{ u})$$
  
= 140.6 MeV

14. One of the simplest fusion reactions involves the production of deuterium, <sup>2</sup><sub>1</sub>H 2.014 102 u, from a neutron and a proton. Write the complete fusion reaction and find the amount of energy released.

$$^{1}P + ^{1}_{0}n \rightarrow ^{2}H$$

$$1(^{1}_{1}P) = 1(1.007 825 u) = 1.007 825$$
  
 $1(^{1}_{2}n) = 1(1.008 665 u) = 1.008 665$   
 $^{2}_{1}H = 2.014 102$   
 $^{2}_{2}H = 2.016 490$ 

mass defect = -0.002388

$$E = (931.5 \text{ MeV/u})(0.002388 \text{ u})$$
  
= 2.224 MeV

## Supplemental Problems

15. The fusion reactions most likely to succeed in a fusion reactor are listed below. Complete each fission reaction.

a. 
$${}^{2}H + {}^{2}H \rightarrow {}^{3}H + ?$$

$$^{2}H + ^{2}H \rightarrow ^{3}H + ^{1}H$$

b. 
$${}_{1}^{2}H + {}_{1}^{2}H \rightarrow {}_{2}^{3}He + ?$$

$${}_{1}^{2}H + {}_{1}^{2}H \rightarrow {}_{2}^{3}He + {}_{0}^{1}n$$

c. 
$${}_{1}^{2}H + {}_{1}^{3}H \rightarrow {}_{2}^{4}He + ?$$

$${}_{1}^{2}H + {}_{1}^{3}H \rightarrow {}_{2}^{4}He + {}_{2}^{1}n$$

d. 
$${}_{1}^{3}H + {}_{1}^{3}H \rightarrow {}_{2}^{4}He + 2?$$

$${}_{1}^{3}H + {}_{1}^{3}H \rightarrow {}_{2}^{4}He + 2({}_{0}^{1}n)$$